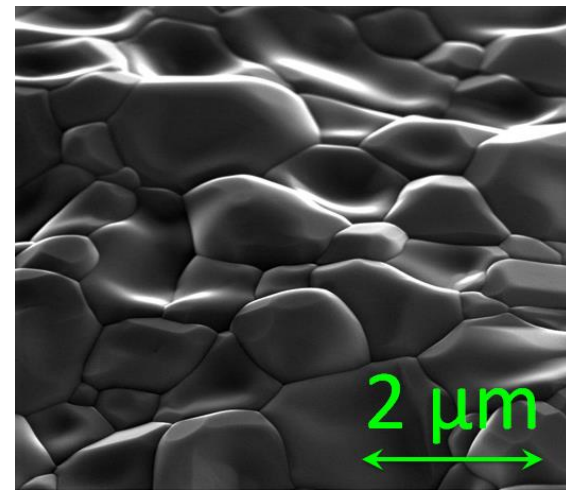
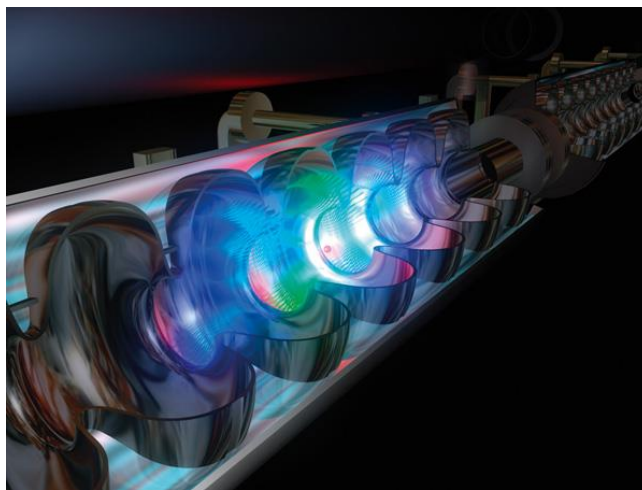
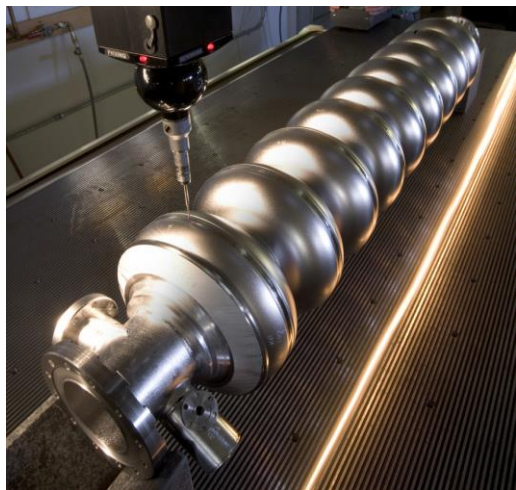


Magnetic Field Limits of Superconducting RF Cavities

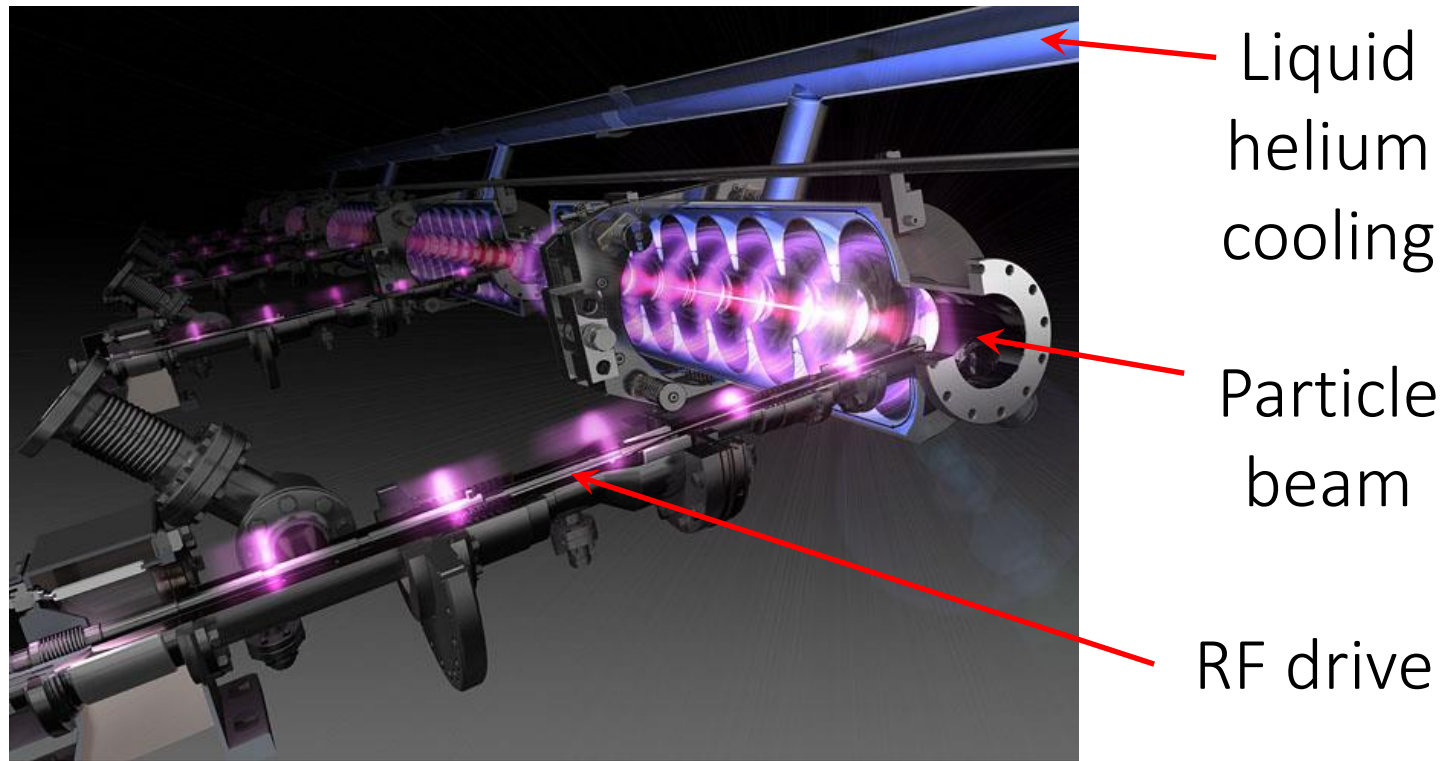


Sam Posen

Associate Scientist, FNAL Technical Division

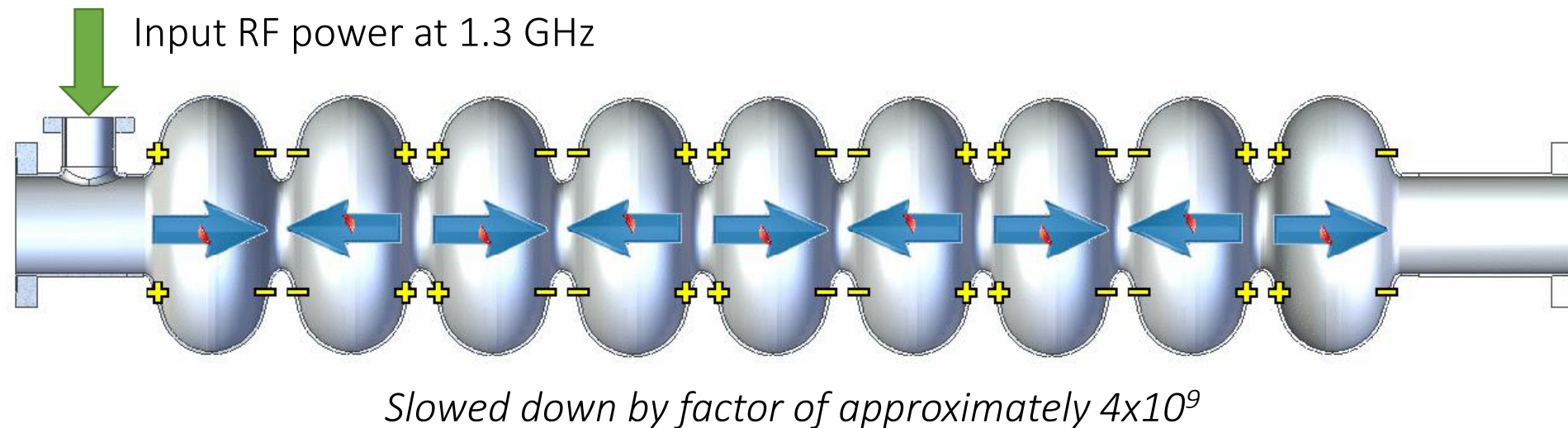
Workshop on Microwave Cavity Design for Axion Detection

August 26, 2015



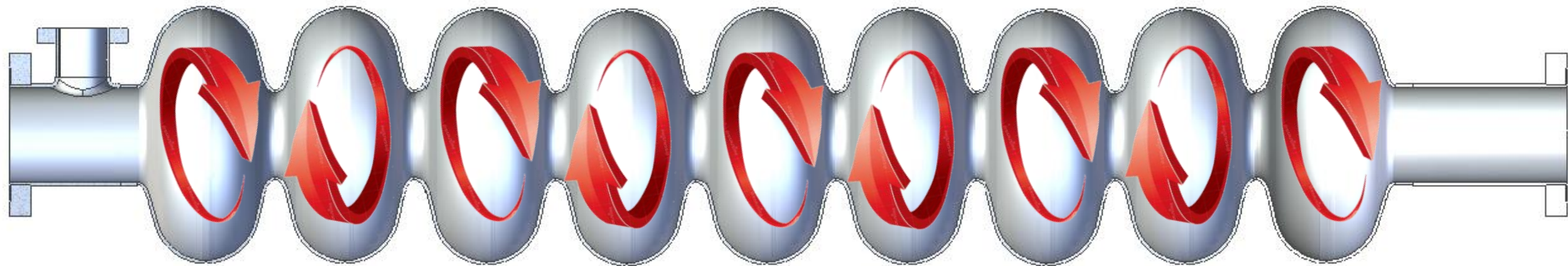
- Muscle of many large particle accelerators
- RF input power \rightarrow accelerating electric field

- SRF cavity: high quality EM resonator
- Particle beam gains energy as it passes through

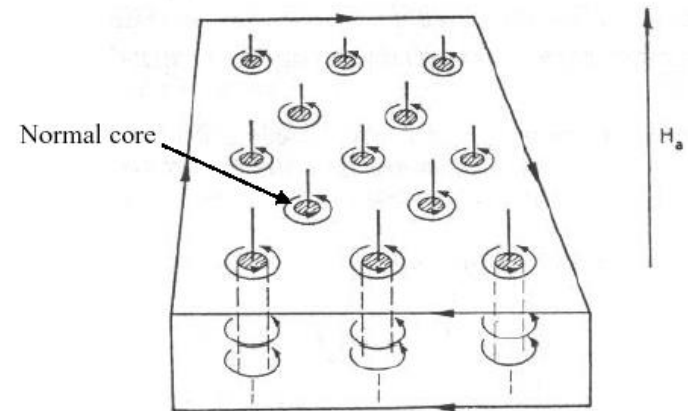
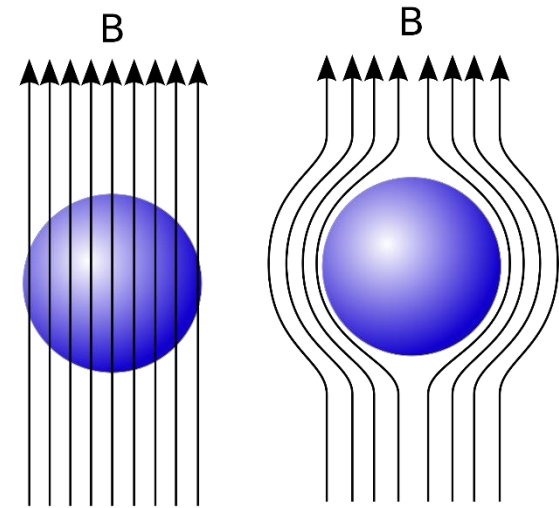


- Electric field provides acceleration
- Magnetic field can't be avoided

- How high in field can we take SRF cavities?
- State of the art niobium cavities are limited by **peak surface magnetic field**



- For relatively small applied magnetic fields, superconductors expel flux: **Meissner state**
- At higher fields, Type II superconductors allow flux to enter in packets: **Vortex state**



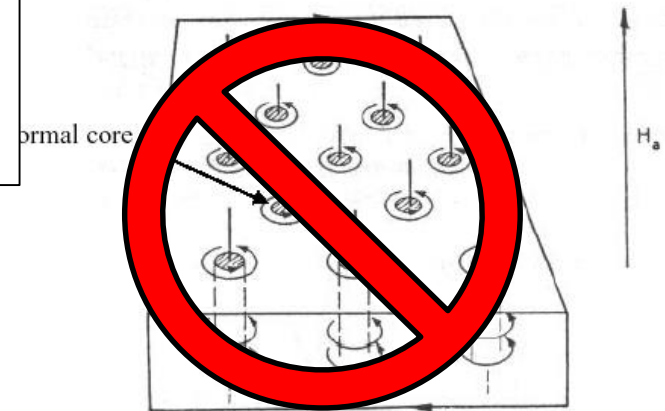
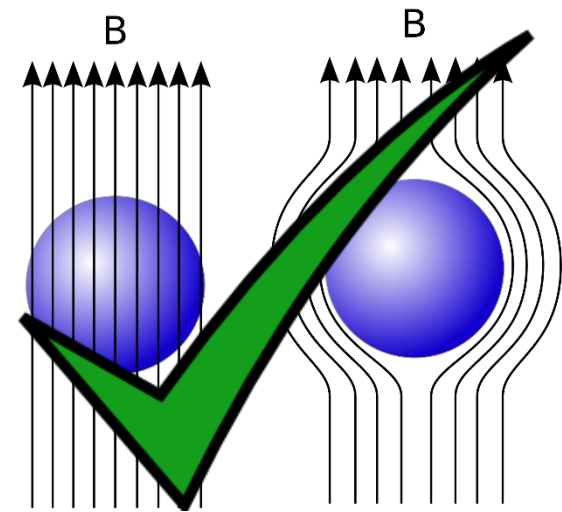
- For relatively small applied magnetic fields, superconductors expel flux: **Meissner state**

Avoid flux penetration.

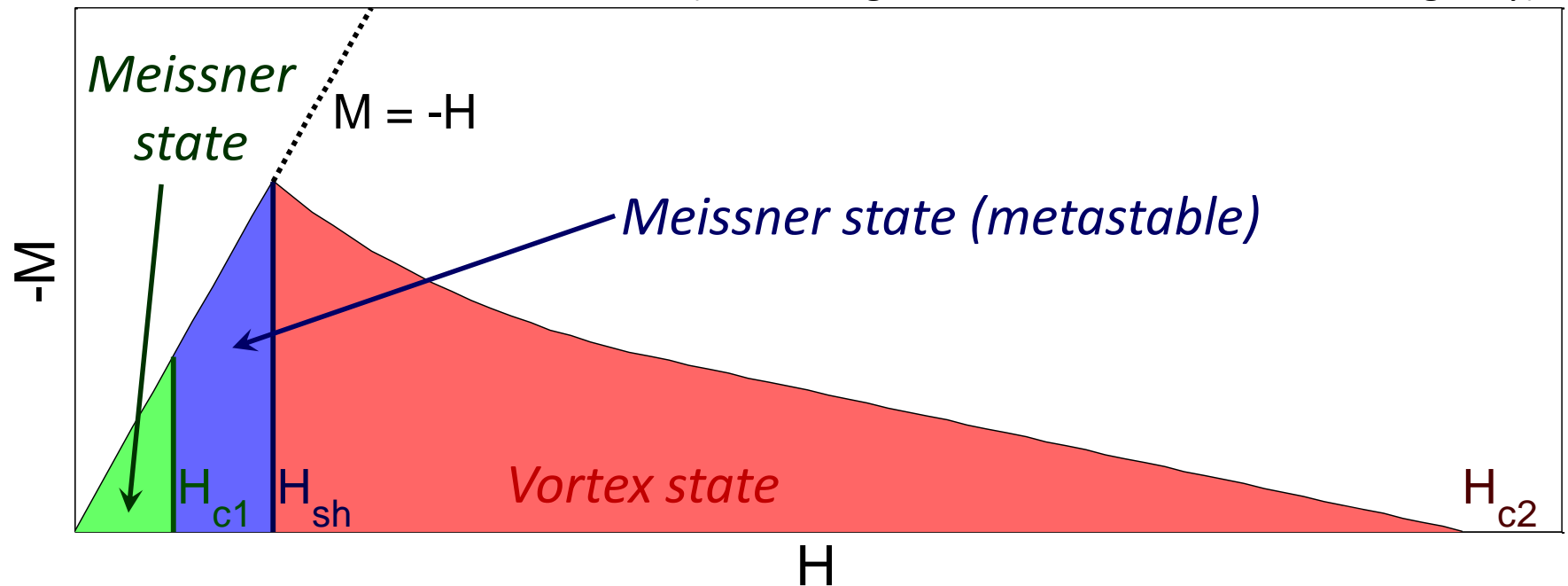
At RF frequencies →

excessive heating

state



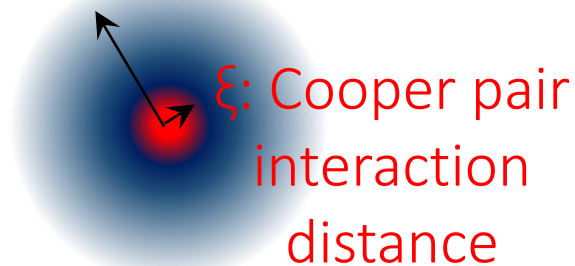
(Note: Magnetization curve for H increasing only)



- Flux free Meissner state is stable up to H_{c1}
- Favorable for flux to be deep in bulk above H_{c1}
- BUT surface energy barrier allows metastable state!

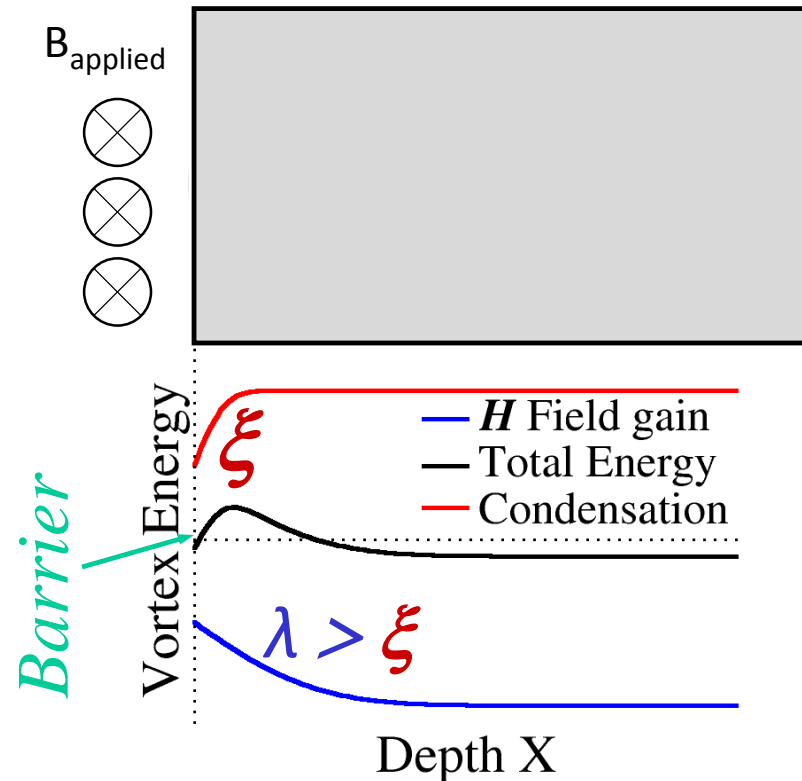
Why a superheating field?

λ : B-field decay constant



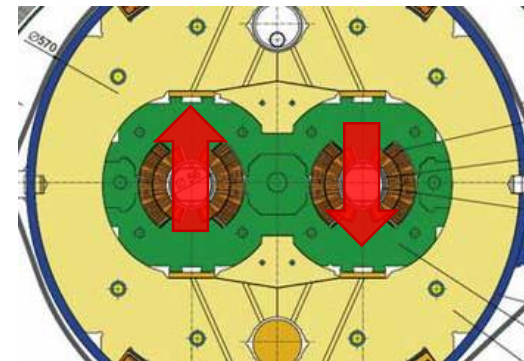
Energy cost: creation of normal conducting vortex core

Energy benefit: flux from high magnetic field region into low magnetic field region



Costly core ξ enters first;
gain from field λ later

- **NbTi** (magnet quality):
 - Lots of pinning centers – $H_{c2} \sim 15 \text{ T}$
 - $T_c \sim 9\text{-}10 \text{ K}$, ductile
- **Niobium** (SRF quality):
 - Robust barrier to magnetic flux – $H_{sh} \sim 0.2 \text{ T}$
 - $T_c \sim 9 \text{ K}$, ductile
- **Nb₃Sn** (can be either!):
 - Can be made with pinning centers – $H_{c2} \sim 30 \text{ T}$
 - Predicted robust barrier to flux – $H_{sh} \sim 0.4 \text{ T?}$
 - $T_c \sim 18 \text{ K}$, brittle



- Used in accelerators: Pb and Nb, either bulk or sputtered
- Many film deposition methods researched: ECR, ALD, CVD, HPCVD, MOCVD, HiPIMS, e-beam, thermal vapor diffusion, liquid diffusion, co-sputtering+annealing, cathodic arc deposition
- Many alternative superconductors considered

Material	$\lambda(0)$ [nm]	$\xi(0)$ [nm]	B_{sh} [mT]	T_c [K]	$\rho_n(0)$ [$\mu\Omega\text{cm}$]
Nb	50	22	210	9.2	2
Nb ₃ Sn	111	4.2	410	18	8
MgB ₂	185	4.9	210	40	0.1
NbN	375	2.9	160	16	144

Parameters for: Nb from [1] assuming $RRR = 10$; Nb₃Sn from [2]; NbN from [3]; MgB₂ from [4] and [5]. B_{sh} for Nb found from equation in [6] and for others calculated from [7]. B_c used to calculate B_{sh} found from [8] eq. 4.20.

[1] B. Maxfield and W. McLean, Phys. Rev. 139, A1515 (1965).

[2] M. Hein, *High-Temperature Superconductor Thin Films at Microwave Frequencies* (Berlin: Springer, 1999).

[3] D. Oates, et al., Phys. Rev. B 43, 7655 (1991).

[4] Y. Wang, T. Plackowski, and A. Junod, Physica C 355, 179 (2001).

[5] X.X. Xi et al., Physica C, 456, 22-37 (2007).

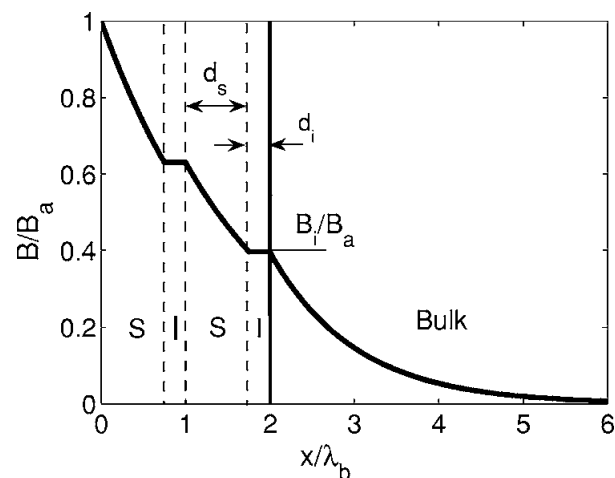
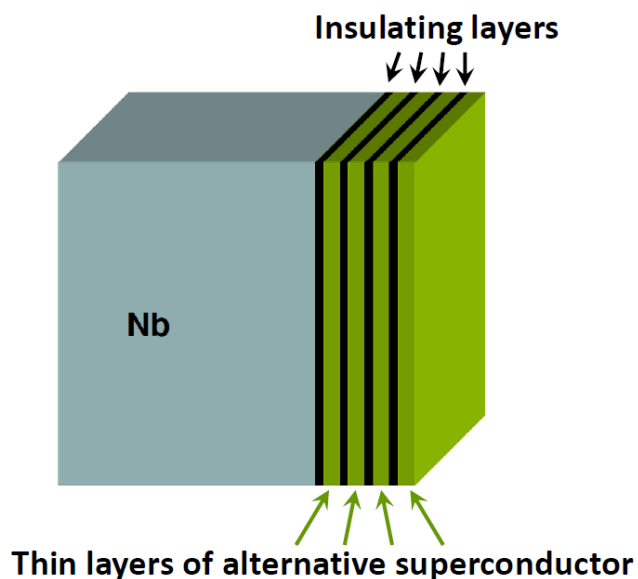
[6] A. Dolgert, S. Bartolo, and A. Dorsey, Erratum [Phys. Rev. B 53, 5650 (1996)], Phys. Rev. B 56, 2883 (1997).

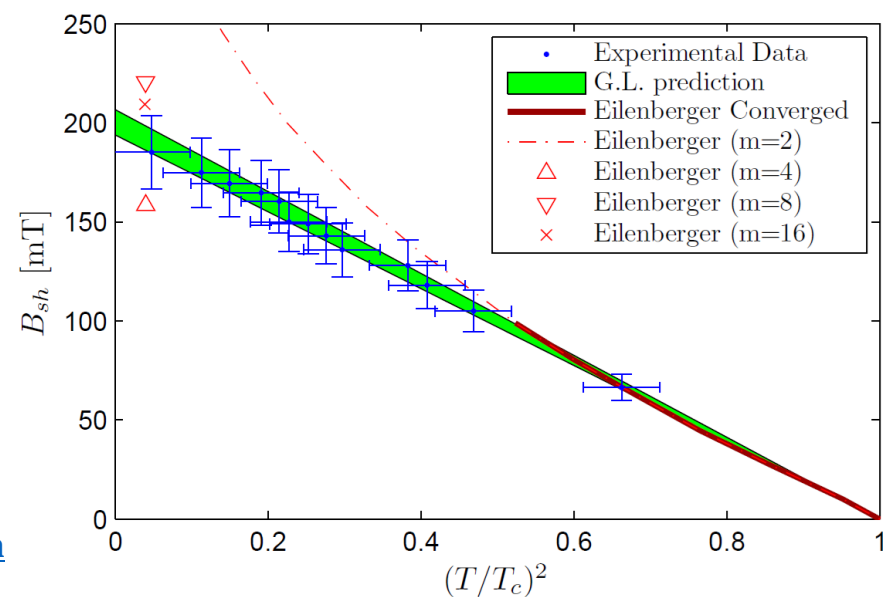
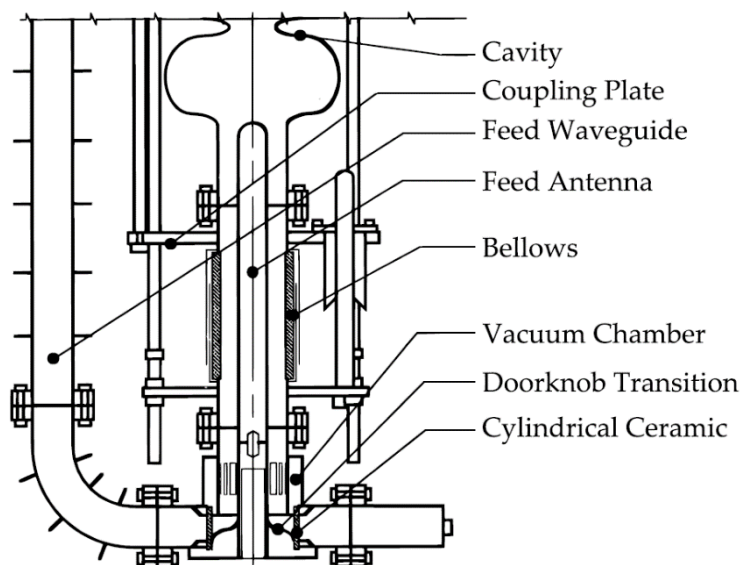
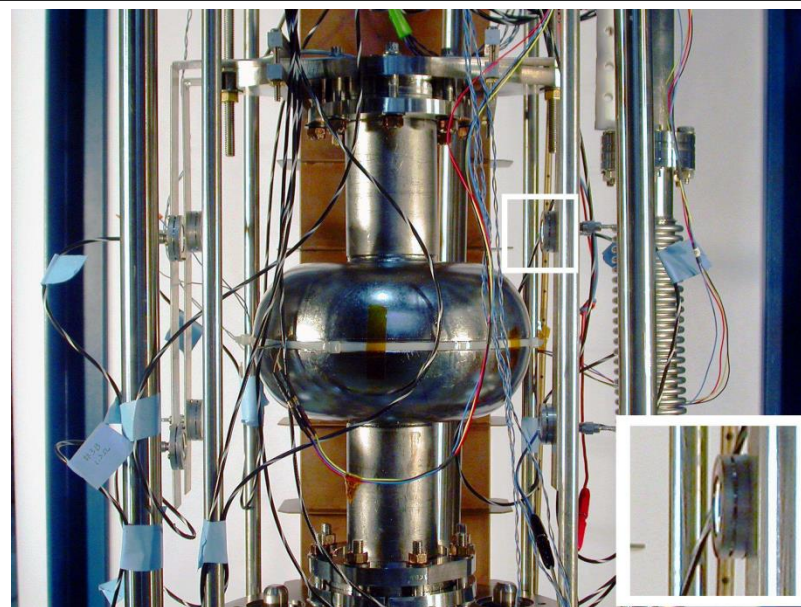
[7] M. Transtrum, G. Catelani, and J. Sethna, Phys. Rev. B 83, 094505 (2011).

[8] M. Tinkham, *Introduction to Superconductivity* (New York: Dover, 1996).

Material parameters vary with fabrication. References were chosen to try to display realistic properties for polycrystalline films.

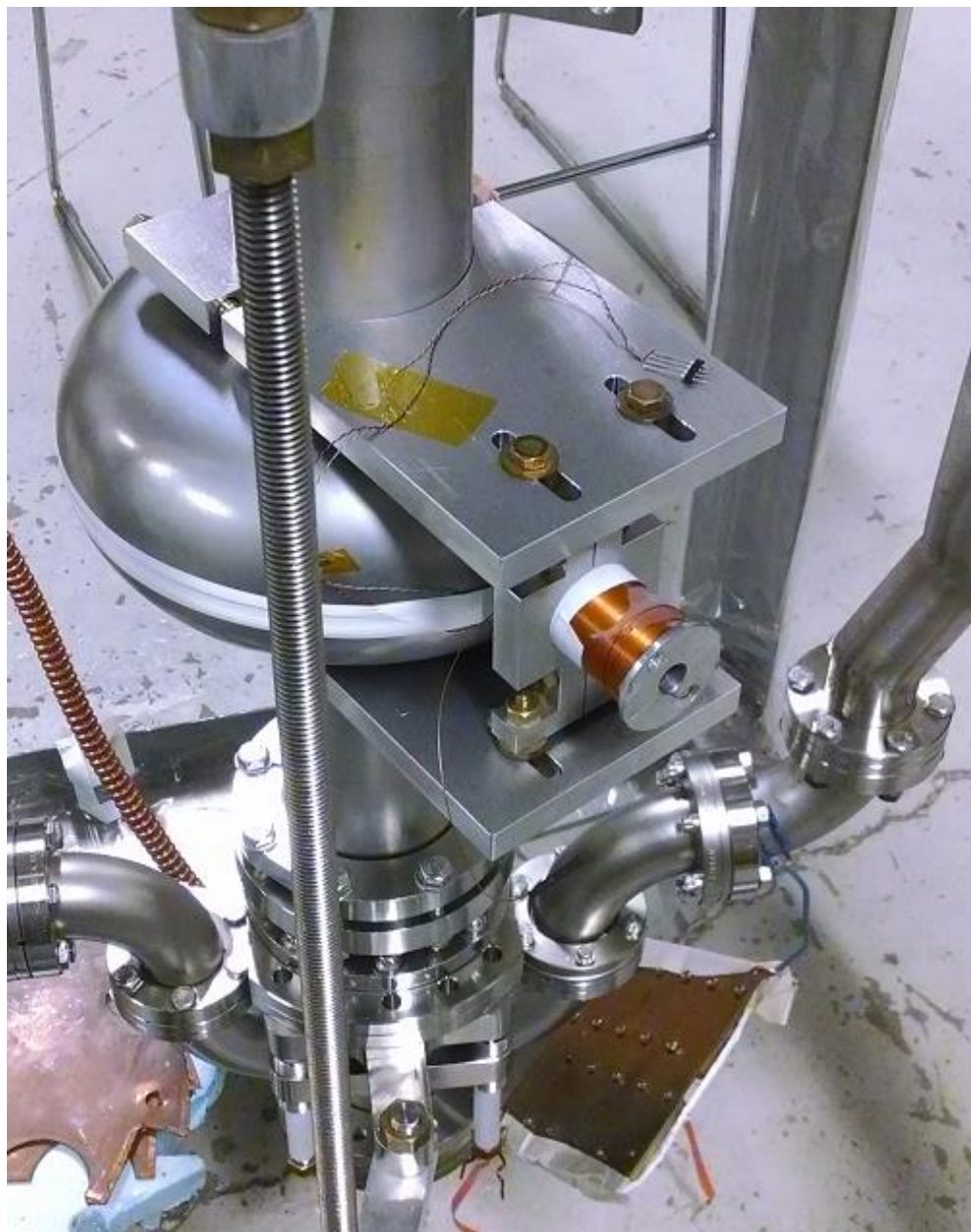
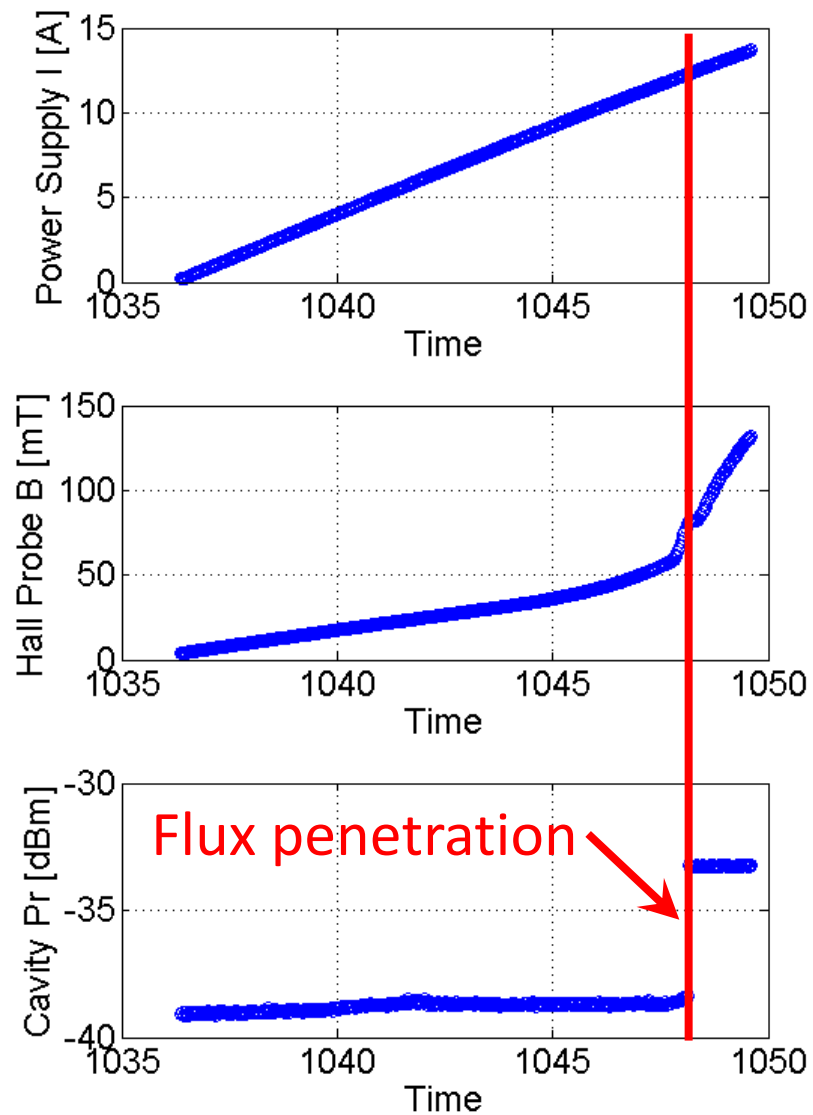
- Alternative geometries considered, including multilayer SIS' films studied in depth
- No significant increase predicted for maximum flux-free field [[Posen et al. 2013](#), [Kubo et al. 2013](#), [Gurevich 2015](#)]

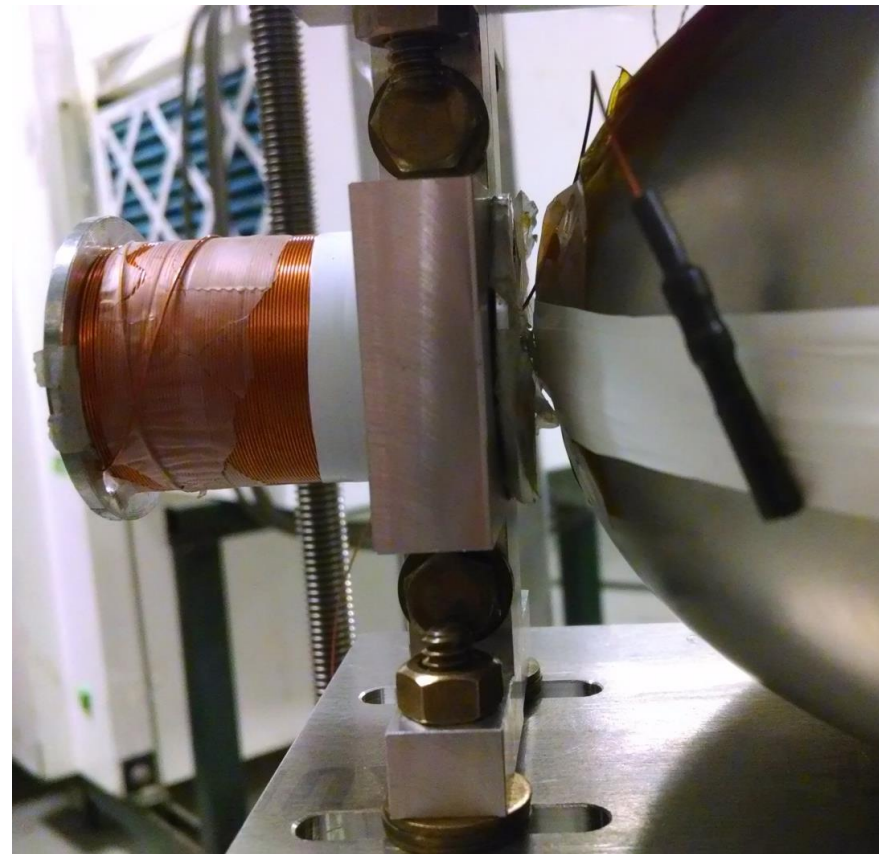
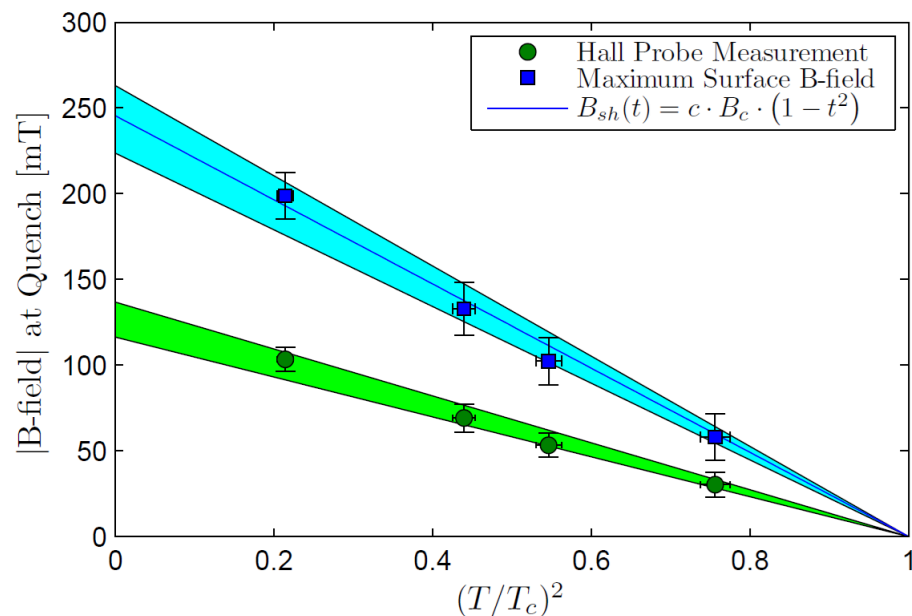
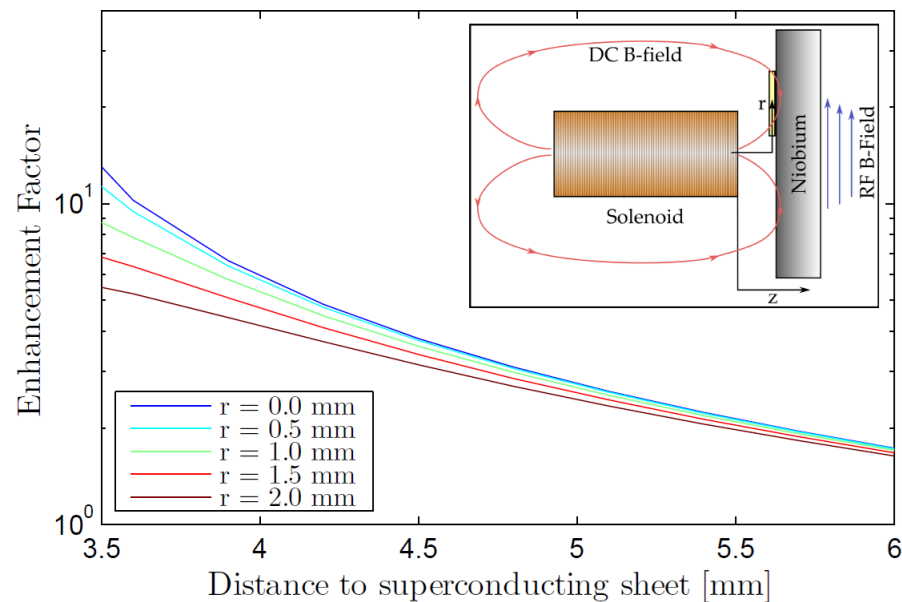




Radio Frequency Magnetic Field Limits of Nb and Nb₃Sn

S. Posen, N. Valles, and M. Liepe, *PRL* 115, 047001 (2015).



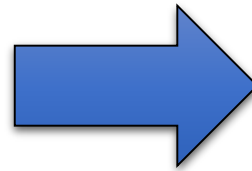


See Nick Valles's thesis,
Cornell University, 2014

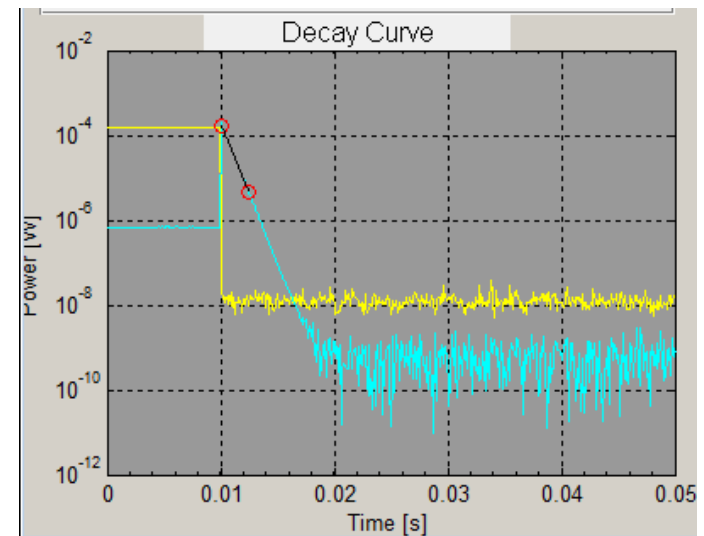
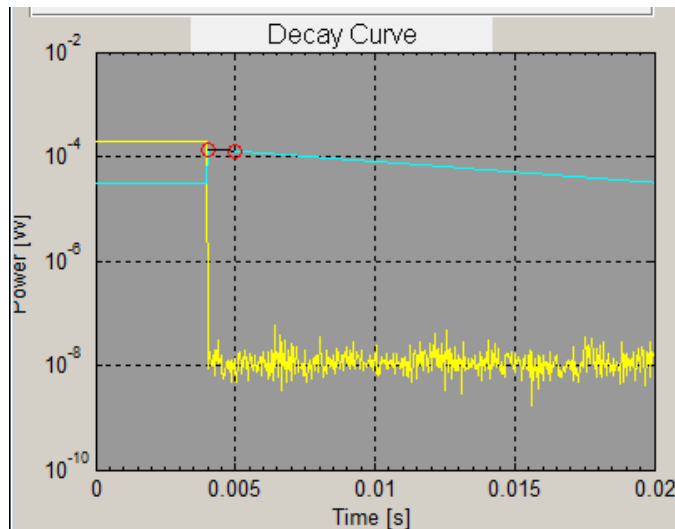
$B_{DC} = 0 \text{ T}$

After $B_{DC} = 0.3 \text{ T}$

Measurement Results	
Quantity	Value
Quality Factor	1.351e+008
Eacc [MV/m]	4.23
Beta_R	0.514
Beta_E	0.525



Measurement Results	
Quantity	Value
Quality Factor	9.908e+006
Eacc [MV/m]	1.07
Beta_R	0.899
Beta_E	0.743



Raw data measured by Nick Valles, Cornell University, 2013

- Realistic expectation: $B_{\text{max}} \sim 0.2 \text{ T}$ at walls of superconducting cavity to maintain high Q_0
- Alternative materials may increase limit up to 0.5 T with a few years of development

- Poloidal field coils
- Large field in cavity interior
- Smaller field at walls

